

9.6

$$\theta(t) = 250 + -20t^2 - 1.5t^3$$

a) $\omega(t) = 0 \Rightarrow t_0 = ?$

$$\rightarrow \omega = \frac{d\theta}{dt} = 250 - 40t - 4.5t^2 = 0$$

$$\therefore t_0 = 4.23 \text{ s}$$

b) $\alpha(t) = ?$ at $t = t_0$

$$\alpha = \frac{d^2\theta}{dt^2} = -40 - 9t = -78 \text{ rad/s}^2$$

c) $\theta(t_0) = ?$

$$\theta = 250 \cdot 4.23 - 20(4.23)^2 - 1.5(4.23)^3 = 586 \text{ rad} \xrightarrow{\frac{1}{2\pi}} 933 \text{ rev}$$

d) $\omega(t=0) = ?$ 250 rad/s

e) $\omega_{\text{av}}(t=0 \rightarrow t=t_0) \rightarrow \frac{\Delta\theta}{\Delta t} = \frac{586}{4.23} \frac{\text{rad}}{\text{s}} = 139 \text{ rad/s}$

9.7 \rightarrow similar

9.26 $r = \frac{0.75 \text{ m}}{2}$ $\omega_0 = 0.25 \frac{\text{rev}}{\text{s}}$ $\alpha = 0.9 \frac{\text{rev}}{\text{s}^2}$

a) $\omega(t=0.2) = ?$ $\omega = \omega_0 + \alpha t = 0.25 + 0.9 \times 0.2 = 0.43 \text{ rev/s}$

b) $\Delta\theta = ?$ $\omega_0 t + \frac{1}{2} \alpha t^2 = 0.25 \times 0.2 + \frac{1}{2} \times 0.9 \times (0.2)^2$
 $= 0.05 + 0.018 = 0.068 \text{ rev}$

c) $v_t = ?$ at $t = 0.2$ $v = \omega \cdot r = 0.43 \times 0.375 \frac{\text{m} \cdot \text{rev}}{\text{s}}$

1 rev = 2π rad $\Rightarrow v = 0.43 \times 0.375 \times 2\pi \approx 1 \text{ m/s}$

d) $a = \sqrt{a_t^2 + a_r^2} = \sqrt{\left(\frac{v^2}{r}\right)^2 + (\alpha \cdot r)^2} = \sqrt{\left(\frac{1}{0.375}\right)^2 + (0.9 \times 2\pi \times 0.375)^2} \approx 35 \frac{\text{m}}{\text{s}^2}$

9.67 $r = 25 \text{ cm}$, $a(t) = At$, $v_0 = 0$, $a(3) = 1.8 \text{ m/s}^2$

a) $A = ? \Rightarrow \frac{a}{t} = A = \frac{1.8}{3} = 0.6 \text{ m/s}^3$

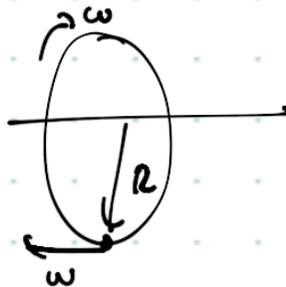
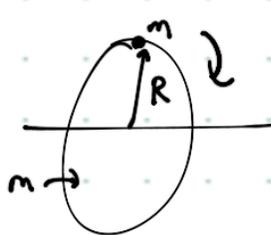
b) $\alpha = ? \quad \alpha = \frac{a}{r} = \frac{0.6t}{0.25} = 2.4t$

c) $\omega(t) = 15 \text{ rad/s} \Rightarrow t = ?$

$$\omega(t) = \int_0^t \alpha(t') dt' = \int_0^t (2.4t') dt' = 15 \Rightarrow 2.4 \frac{t^2}{2} = 15 \Rightarrow t = \sqrt{\frac{30}{2.4}} \approx 3.5 \text{ s}$$

d) $\theta(3.5) = ? \quad \theta = \int_0^t \omega(t') dt' = \frac{1.2 t^3}{3} = 0.4 t^3 = 0.4 (3.5)^3 \approx 18 \text{ rad}$

9.80



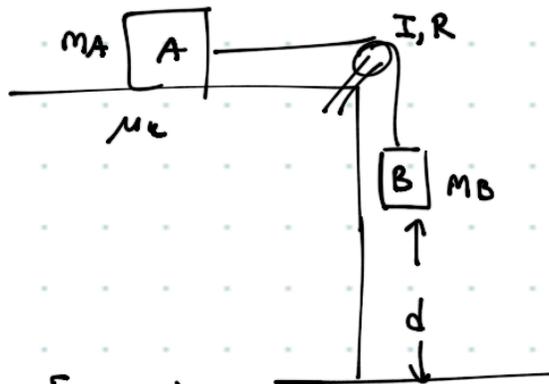
$$I_1 = I_{\text{dix}} = \frac{1}{2} m R^2$$

$$I_2 = I_{\text{obj}} = m R^2$$

$$E_i = E_f \Rightarrow mg \cdot 2R = \frac{1}{2} I_1 \omega^2 + \frac{1}{2} I_2 \omega^2 = \frac{3}{4} m R^2 \omega^2$$

$$\therefore \omega^2 = \frac{8g}{3R}$$

9.85

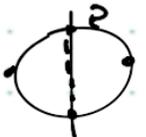


$v = ?$

$$E_i = E_f \Rightarrow$$

$$m_B g d - \mu_k (m_A g) \cdot d = \frac{1}{2} (m_A + m_B) v^2 + \frac{1}{2} I \frac{v^2}{R^2}$$

$$\therefore g d [m_B - \mu_k m_A] = \frac{v^2}{2} \left[m_A + m_B + \frac{I}{R^2} \right] \Rightarrow v = \sqrt{\frac{2 g d (m_B - \mu_k m_A)}{m_A + m_B + \frac{I}{R^2}}}$$

10.8 $m = 8.4 \text{ kg}$ $r = 25 \text{ cm}$ 4 small $m = 2 \text{ kg}$ masses  $\tau_{\text{Friction}} = ?$ $\omega_i = 75 \text{ rpm}$ $\omega_f = 50 \text{ rpm}$ $\Delta t = 30 \text{ s}$

$\tau = I \alpha$ Calculate $I, \alpha \rightarrow$ get $\tau!$
 $\uparrow_{\text{const}} \rightarrow \uparrow_{\text{const}}$

$$I = I_{\text{sphere}} + I_{\text{balls}} = \frac{2}{3} MR^2 + 2mR^2 = 2R^2 \left[\frac{M}{3} + m \right] = 2 \cdot (0.25)^2 \left[\frac{8.4}{3} + 2 \right]$$

$$\frac{\Delta \omega}{\Delta t} = \alpha = \frac{50 - 75}{30} \frac{\text{rev}}{\text{min}} \cdot \frac{1}{\text{s}} \Rightarrow -\frac{25}{30} \cdot \frac{2\pi}{60} \frac{\text{rad}}{\text{s}^2} \approx -0.09$$

$$\rightarrow \tau = 0.6 \times -0.09 \approx -0.54 \text{ Nm}$$

10.29 $m = 1.5 \text{ kg}$, $r = 0.1 \text{ m}$,

a) $\tau = ?$ $\omega_0 = 0$ $\omega_f = 1200 \frac{\text{rev}}{\text{min}}$ $\Delta t = 2.5 \text{ s}$

$\tau \rightarrow \text{const}$, $\alpha \rightarrow \text{const}$

$$\therefore \omega_f = \omega_0 + \alpha \Delta t \Rightarrow$$

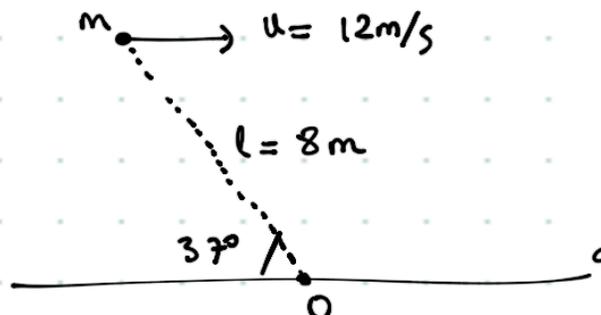
$$\alpha = \frac{1200 \cdot 2\pi}{60 \cdot 2.5} \approx 50 \text{ rad/s}^2$$

$$\tau = I \alpha = \frac{1}{2} \cdot 1.5 \cdot (0.1)^2 \cdot 50 \approx \frac{1.5}{4} \approx 0.375 \text{ N}\cdot\text{m}$$

b) $\Delta \theta = ?$ $\theta = \omega_0 t + \frac{1}{2} \alpha t^2 = \frac{1}{2} \cdot 50 \cdot (2.5)^2 = \frac{50 \cdot 25}{8} = \frac{625}{4} \approx 156 \text{ rad}$

c) $W = \vec{F} \cdot \Delta \vec{x} \Rightarrow \tau \cdot \Delta \theta = 0.375 \times 156 \approx 59 \text{ Joule}$ ← same

d) $K = \frac{1}{2} I \omega^2 = \frac{1}{2} \times \frac{1}{2} \times 1.5 \times (0.1)^2 \times \left(\frac{1200 \cdot 2\pi}{60} \right)^2 = 1.5 \times 4\pi^2 \approx 60 \text{ Joule}$

10.35 

$m = 2 \text{ kg}$; $\vec{L}_0 = ?$

$$\vec{r} \times \vec{p} = 8 \times 2 \times 12 \times \frac{3}{5}$$

a) $L = \frac{48 \times 12}{5} \approx 115$ \otimes

b) $\frac{d\vec{L}}{dt} = \vec{\tau}$ along $m \rightarrow O$

out of the page \otimes Torque



into the page \otimes
 $mg \cdot l \cos \theta = 2 \cdot 8 \cdot \frac{4}{5} \approx 128$

10.36 $m = 12 \text{ kg}$ $r = 24 \text{ cm}$ $\theta(t) = At^2 + Bt^4$ $A = 1.5$, $B = 1.1$

a) units of A, B b) $L(3) = ?$, $\tau(3) = ?$

$L = I\omega$ for rotation : $\frac{dL}{dt} = \tau = I\alpha$

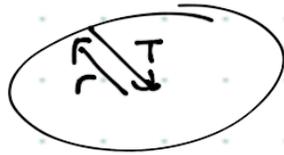
$\therefore \omega(t) = \frac{d}{dt} \{At^2 + Bt^4\} = 2At + 4Bt^3$

$\therefore L = I \{2At + 4Bt^3\}$ $\tau = \frac{d}{dt} L = I \{2A + 12Bt^2\}$

* 10.40 $m = 0.025 \text{ kg}$, $r_0 = 0.3 \text{ m}$, $\omega_0 = 1.75 \text{ rad/s}$

$\rightarrow r_f = 0.15 \text{ m}$

a) $\vec{\tau} = \vec{r} \times \vec{T} = 0$



$\therefore \frac{d\vec{L}}{dt} = 0$

$\therefore \omega_f = 7 \text{ rad/s}$

b) $L_i = L_f$

$\rightarrow m v_i r_i = m v_f r_f$

$\Rightarrow 1.75 \times \frac{0.3}{4} \times 0.3 = \omega_f \cdot (0.15)^2$

c) $\Delta KE = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2 = \frac{1}{2} m \{ [7(0.15)]^2 - [1.75 \times 0.3]^2 \}$

$= \frac{1}{2} \times 0.025 \times (1.75 \times 0.3)^2 [4 - 1] = \frac{1}{2} \times \frac{25}{10} \times 10^{-3} \times \underbrace{(1.75)^2}_{\sim 3} \cdot 3 \cdot \underbrace{(0.3)^2}_{0.1} \sim 0.01$

d) $w = \Delta KE$