

## GROUP DECISION MAKING UNDER MULTIPLE CRITERIA

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### FINAL EXAM

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You may use lecture notes and other related printed sources as well as your computer for soft documents and mathematical calculations. You should turn off internet property of the computer.

Duration: 3 hours

### QUESTIONS

1. (10 points) What are the differences between process oriented approaches and content oriented approaches? Is it possible to integrate the concept of process and content oriented approaches for some kind of problems?
2. Suppose a hypothetical city, Tekelonya, where 895,151 votes are cast for five party lists contesting five seats and suppose the distribution of votes is as follows:

|                       |         |
|-----------------------|---------|
| Journey Party         | 182,557 |
| Bribe Lovers Party    | 362,191 |
| Movement Party        | 114,697 |
| Winter Sleep Party    | 52,342  |
| Jobs and Powers Party | 183,364 |

- a. (15 Points) Allocate seats to party lists by using D' Hondt's rule and Greatest remainder method with droop quota. Compare the results based on the characteristic of the methods.
  - b. (10 Points) Proportional representation (PR) is a concept in non-ranked voting systems used to elect two or members. PR means that the number of seats won by a party or group of candidates is proportionate to the number of votes received. Formulate a mathematical programming model for the given example to determine the number of seats according to the concept of proportional representation.
3. (20 Points) Suggest a classification scheme for explicit group decision making approaches. Classify the following papers, which are analyzed in the class, accordingly.
    - A.İ. Ölçer, A.Y. Odabaşı, A new fuzzy multiple attributive group decision making methodology and its application to propulsion/manoeuvring system selection problem, European Journal of Operational Research, Volume 166, Issue1, 2005, Pages93-114
    - Xu, Z. (2004) Uncertain linguistic aggregation operators based approach to multiple attribute group decision making under uncertain linguistic environment, Information Sciences 168, 171–184
    - Ignacio Javier Pérez, Francisco Javier Cabrerizo, and Enrique Herrera-Viedma, A Mobile Decision Support System for Dynamic Group Decision-Making Problems, IEEE Transactions ON Systems, Man, and Cybernetics—Part A: Systems and humans, VOL. 40, NO. 6, 2010

4. Brown family is planning to buy a new car. On their decision to determine the model of the car, they have specified three alternatives: BMW 316i, Mercedes C180, and Audi A4. In order to make the final decision family members evaluated the alternatives in pairwise manner using Saaty's scale as in the following tables.
- (12 Points) Use a soft consensus measure to find the weights of the family members, and aggregate the evaluations based on these weights.
  - (13 Points) Use a soft proximity measure to find proximity of each family member to the aggregate score.

| Mr. Brown     | BMW 316 | Mercedes C180 | Audi A4 |
|---------------|---------|---------------|---------|
| BMW 316       | 1       | 5             | 7       |
| Mercedes C180 | 1/5     | 1             | 2       |
| Audi A4       | 1/7     | 1/2           | 1       |

| Mrs. Brown    | BMW 316 | Mercedes C180 | Audi A4 |
|---------------|---------|---------------|---------|
| BMW 316       | 1       | 1/5           | 1/4     |
| Mercedes C180 | 5       | 1             | 1/3     |
| Audi A4       | 4       | 3             | 1       |

| Yellow        | BMW 316 | Mercedes C180 | Audi A4 |
|---------------|---------|---------------|---------|
| BMW 316       | 1       | 1             | 1/3     |
| Mercedes C180 | 1       | 1             | 1/4     |
| Audi A4       | 3       | 4             | 1       |

5. (25 points) A software company desires to hire a system analysis engineer among three candidates A1, A2 and A3 who are evaluated by a committee of 3 decision makers against three benefit criteria; i.e. emotional steadiness (C1), oral communication skills (C2), personality (C3). The relative importance weights of 3 criteria are described using linguistic variables such as Low, Medium etc. (see Table 1). Ratings (i.e. criteria values) are also characterized by linguistic variables such as Poor, Fair, Good as (see Table 2)

**Table 1.**

| Linguistic variables | Fuzzy Number    |
|----------------------|-----------------|
| Very low (VL)        | (0,0,0.1)       |
| Low(L)               | (0,0.1,0.3)     |
| Med. L(ML)           | (0.1, 0.3, 0.5) |
| Med.(M)              | (0.3, 0.5, 0.7) |
| Med. High (MH)       | (0.5,0.7,0.9)   |
| High (H)             | (0.7, 0.9, 1.0) |
| Very High (VH)       | (0.9, 1.0, 1.0) |

**Table 2.**

| Linguistic variables | Fuzzy Number |
|----------------------|--------------|
| Very Poor(VP)        | (0,0,1)      |
| Poor(P)              | (0,1,3)      |
| Medium Poor (MP)     | (1,3,5)      |
| Fair (F)             | (3,5,7)      |
| Med.Good (MG)        | (5,7,9)      |
| Good (G)             | (7,9,10)     |
| Very Good (VG)       | (9,10,10)    |

Three DMs Express their opinions on the importance weights of the 3 criteria and their ratings of each candidate with respect to 3 criteria are given individually (see Table 3 and Table 4 respectively).

**Table 3.**

| Criterion | DM1 | DM2 | DM3 |
|-----------|-----|-----|-----|
| C1        | H   | VH  | MH  |
| C2        | VH  | VH  | VH  |
| C3        | VH  | H   | H   |

**Table 4.**

| Criterion | Candidate | DM1 | DM2 | DM3 |
|-----------|-----------|-----|-----|-----|
| <b>C1</b> | A1        | MG  | MG  | MG  |
|           | A2        | G   | MG  | MG  |
|           | A3        | VG  | MG  | F   |
| <b>C2</b> | A1        | G   | MG  | F   |
|           | A2        | VG  | VG  | VG  |
|           | A3        | MG  | G   | VG  |
| <b>C3</b> | A1        | F   | G   | G   |
|           | A2        | VG  | VG  | G   |
|           | A3        | G   | MG  | VG  |

The importance of decision makers for the evaluation of the candidates according to three criteria are given in Table 5.

**Table 5.**

|           | Importance of Decision Makers |      |     |
|-----------|-------------------------------|------|-----|
| Criterion | DM1                           | DM2  | DM3 |
| <b>C1</b> | 0.3                           | 0.5  | 0.4 |
| <b>C2</b> | 1                             | 0.6. | 0.3 |
| <b>C3</b> | 0.7                           | 1    | 1   |

Find the most appropriate candidate according to aggregated group decision, using an appropriate fuzzy group decision making approach which depends on an outranking MADM method. (You may use an existing method analyzed in the class or create a new one)

GOOD LUCK!