

$$c(\theta) \equiv \cos(\theta) \qquad s(\theta) \equiv \sin(\theta)$$

$$\mathbf{P}_1 := \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} \quad \mathbf{P}_2 := \begin{pmatrix} 0 \\ 5 \\ 0 \end{pmatrix} \quad n := \frac{P_2 - P_1}{|P_2 - P_1|} \quad n = \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \quad \begin{pmatrix} n_x \\ n_y \\ n_z \end{pmatrix} := n$$

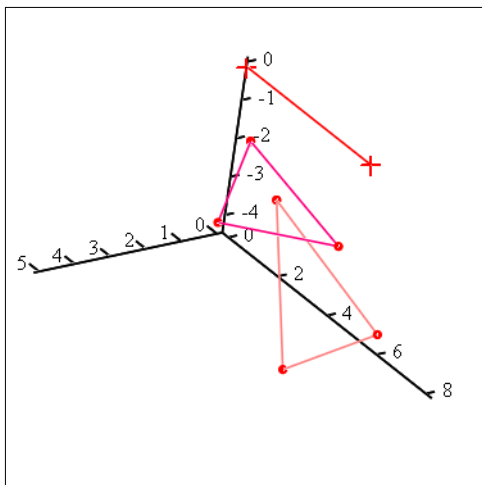
$$\begin{array}{lll} \mathbf{P} := \begin{pmatrix} 2 & 5 & 3 & 2 \\ 3 & 6 & 8 & 3 \\ 0 & 0 & 0 & 0 \end{pmatrix} & \mathbf{i} := 0 \dots \text{cols}(\mathbf{P}) - 1 & \mathbf{G} := \text{augment}(\mathbf{P}_1, \mathbf{P}_2) \\ & & \mathbf{G} := \mathbf{G}^T \end{array}$$

$$R(\theta) := \begin{bmatrix} n_X^2 \cdot (1 - c(\theta)) + c(\theta) & n_X \cdot n_Y \cdot (1 - c(\theta)) - n_Z \cdot s(\theta) & n_X \cdot n_Z \cdot (1 - c(\theta)) + n_Y \cdot s(\theta) \\ n_X \cdot n_Y \cdot (1 - c(\theta)) + n_Z \cdot s(\theta) & n_Y^2 \cdot (1 - c(\theta)) + c(\theta) & n_Y \cdot n_Z \cdot (1 - c(\theta)) - n_X \cdot s(\theta) \\ n_X \cdot n_Z \cdot (1 - c(\theta)) - n_Y \cdot s(\theta) & n_Y \cdot n_Z \cdot (1 - c(\theta)) + n_X \cdot s(\theta) & n_Z^2 \cdot (1 - c(\theta)) + c(\theta) \end{bmatrix}$$

$$R\left(\frac{\pi}{3}\right) = \begin{pmatrix} 0.5 & 0 & 0.866 \\ 0 & 1 & 0 \\ -0.866 & 0 & 0.5 \end{pmatrix} \quad p(\theta) := R(\theta) \cdot P \quad p(\theta) = \begin{pmatrix} 1 & 2.5 & 1.5 & 1 \\ 3 & 6 & 8 & 3 \\ -1.732 & -4.33 & -2.598 & -1.732 \end{pmatrix}$$

$$X := \left[(P)^T \right]^{\langle 0 \rangle} \quad Y := \left[(P)^T \right]^{\langle 1 \rangle} \quad Z := \left[(P)^T \right]^{\langle 2 \rangle}$$

$$\mathbf{x} := \left(p(\theta)^T \right)^{\langle 0 \rangle} \quad \mathbf{y} := \left(p(\theta)^T \right)^{\langle 1 \rangle} \quad \mathbf{z} := \left(p(\theta)^T \right)^{\langle 2 \rangle}$$



$$(G^{\langle 0 \rangle}, G^{\langle 1 \rangle}, G^{\langle 2 \rangle}), (X, Y, Z), (x, y, z)$$

$$\text{m}:=10 \quad \text{j}:=0.. \text{m} \quad \text{s}_{\text{j}}:=\frac{2\cdot \pi \cdot \text{j}}{\text{m}} \qquad \theta_{\text{j}}:=\frac{2\cdot \pi \cdot \text{j}}{\text{m}} \qquad \text{c}(\theta)\equiv \cos(\theta) \qquad \text{s}(\theta)\equiv \sin(\theta)$$

$$\text{k}:=0..2$$

$$\text{P}_1:=\begin{pmatrix}0\\0\\0\end{pmatrix} \qquad \text{P}_2:=\begin{pmatrix}0\\5\\0\end{pmatrix} \qquad \text{n}:=\frac{\text{P}_2-\text{P}_1}{\left|\text{P}_2-\text{P}_1\right|} \qquad \text{n}=\begin{pmatrix}0\\1\\0\end{pmatrix} \qquad \begin{pmatrix}\text{n}_{\text{x}}\\ \text{n}_{\text{y}}\\ \text{n}_{\text{z}}\end{pmatrix}:=\text{n} \qquad \text{G}:=\text{augment}(\text{P}_1,\text{P}_2)$$

$$\text{G}:=\text{G}^{\text{T}}$$

$$\text{P}:=\begin{pmatrix}2&5&3&2\\3&6&8&3\\0&0&0&0\end{pmatrix} \qquad \text{i}:=0.. \text{cols}(\text{P})-1$$

$$\text{R}(\theta):=\begin{bmatrix} \text{n}_{\text{x}}^2\cdot(1-\text{c}(\theta))+\text{c}(\theta) & \text{n}_{\text{x}}\cdot\text{n}_{\text{y}}\cdot(1-\text{c}(\theta))-\text{n}_{\text{z}}\cdot\text{s}(\theta) & \text{n}_{\text{x}}\cdot\text{n}_{\text{z}}\cdot(1-\text{c}(\theta))+\text{n}_{\text{y}}\cdot\text{s}(\theta) \\ \text{n}_{\text{x}}\cdot\text{n}_{\text{y}}\cdot(1-\text{c}(\theta))+\text{n}_{\text{z}}\cdot\text{s}(\theta) & \text{n}_{\text{y}}^2\cdot(1-\text{c}(\theta))+\text{c}(\theta) & \text{n}_{\text{y}}\cdot\text{n}_{\text{z}}\cdot(1-\text{c}(\theta))-\text{n}_{\text{x}}\cdot\text{s}(\theta) \\ \text{n}_{\text{x}}\cdot\text{n}_{\text{z}}\cdot(1-\text{c}(\theta))-\text{n}_{\text{y}}\cdot\text{s}(\theta) & \text{n}_{\text{y}}\cdot\text{n}_{\text{z}}\cdot(1-\text{c}(\theta))+\text{n}_{\text{x}}\cdot\text{s}(\theta) & \text{n}_{\text{z}}^2\cdot(1-\text{c}(\theta))+\text{c}(\theta) \end{bmatrix}$$

$$\text{D}:=\left|\left(\text{P}^{\langle 0 \rangle}-\text{P}_1\right)\times \text{n}\right| \qquad \text{D}=2$$

$$\text{d}_{\text{k},\text{i}}:=\left[\left(\text{P}^{\langle \text{i} \rangle}-\text{P}_1\right)\times \text{n}\right]_{\text{k}} \qquad \text{d}=\begin{pmatrix}0&0&0&0\\0&0&0&0\\2&5&3&2\end{pmatrix}$$

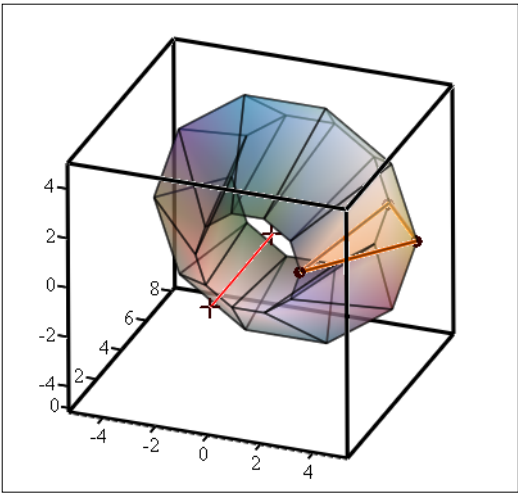
$$\text{T}_{\text{k}}:=\begin{pmatrix}1&0&\text{d}_{\text{k},0}\\0&1&\text{d}_{\text{k},1}\\0&0&\text{d}_{\text{k},2}\end{pmatrix} \quad \text{T1}_{\text{k}}:=\begin{pmatrix}1&0&-\text{d}_{\text{k},0}\\0&1&-\text{d}_{\text{k},1}\\0&0&-\text{d}_{\text{k},2}\end{pmatrix} \qquad \text{T}_1=\begin{pmatrix}1&0&0\\0&1&0\\0&0&0\end{pmatrix}$$

$$\text{p}(\theta):=\text{R}(\theta)\cdot \text{P}$$

$$\text{R}\left(\frac{\pi}{3}\right)=\begin{pmatrix}0.5&0&0.866\\0&1&0\\-0.866&0&0.5\end{pmatrix}$$

$$X := \left[(P)^T \right]^{\langle 0 \rangle T} \qquad Y := \left[(P)^T \right]^{\langle 1 \rangle T} \qquad Z := \left[(P)^T \right]^{\langle 2 \rangle T}$$

$$x_{j,i} := \left[\left[\left((p(\theta_j)) \right)^T \right]^{\langle 0 \rangle T} \right]_{0,i} \qquad y_{j,i} := \left[\left[\left((p(\theta_j)) \right)^T \right]^{\langle 1 \rangle T} \right]_{0,i} \qquad z_{j,i} := \left[\left[\left((p(\theta_j)) \right)^T \right]^{\langle 2 \rangle T} \right]_{0,i}$$



$$\left(G^{\langle 0 \rangle}, G^{\langle 1 \rangle}, G^{\langle 2 \rangle} \right), (X, Y, Z), (x, y, z)$$

$$\left[\left[\left((p(\theta_j)) \right)^T \right]^{\langle 2 \rangle T} \right]_{0,i} =$$

0
-1.176
-1.902
-1.902
-1.176
0
1.176
1.902
1.902
1.176
0
0
-2.939
-4.755
-4.755
...

$$p_{j,k} := T_k \cdot R(\theta_j) \cdot T1_k \cdot p^{\langle k \rangle}$$

$$x_{j,i} := \left(T_{\textcolor{red}{k}} \cdot R(\theta_j) \cdot T1_k \cdot p^{\langle k \rangle} \right)_{0,i}$$