

Digital Circuits		
 b) Moore Model Edward Forrest Moore (1925-2003) Mathema In this model, the output depends only on the Input values determine only the next state. And the state determines the output. O = G(S) 	current state.	
inpute excitation	$\begin{array}{c} \text{current} \\ \text{state (S)} \\ \hline \\ $	
clock signal		
Most sequential circuits can be designed using e or Moore).	ither one of these models (Mealy	
Next States in Mealy and Moore models: In both models, next state S^+ is determined by a function H, which is a combination of function F and characteristic equations of the flip-flops. $S^+ = H(I,S)$		
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Digital Circuits

Analysis of clocked synchronous sequential circuits

Before we start to design sequential circuits, we will see how to analyze a given sequential circuit.

Reminder: Implementation of a sequential circuit means implementation of the functions F (flip-flop excitation) and G (output). (See 9.1 and 9.2)

I: Input, S: Current State, S⁺: Next state, O : Output

 $S^+ = H(I,S)$, Mealy: O = G(I,S) Moore: O = G(S)

Analyzing a synchronous circuit means determining the behavior of the circuit (i.e., answering the question "What does the circuit do?"), which is given by the functions F and G .

The analysis of a synchronous circuit consists of five steps:

1. Determine the expressions of the function F (inputs of flip-flops).

2. Use F and characteristic equations of the flip-flops to find the expression of H.

3. Construct the state table that specifies the next state of the circuit for every

possible combination of input and current state.

4. Determine the expressions of the output function G.

5. Determine the output values using G, and construct the state/output table. (Optional) To see the behavior of the circuit better, draw the state diagram (also

called a state graph), which shows all state transitions and outputs of the machine graphically. http://akademi.itu.edu.tr/en/buzluca/ http://www.buzluca.info 2011 – 2023 Feza BUZLUCA 9.3

Digital Circuits

Determination of next states (function H):

The **F** function of a clocked sequential circuit determines the input values of the flip-flops (flip-flop excitation).

These input values, along with the current state of the flip-flop, determine the next state of the flip-flop (i.e., the output of the flip-flop after the transition of the clock signal) (Slides 9.1 and 9.2).

$S^+ = \mathbf{H}(I,S)$

Function H is a combination of function F and characteristic equations of the flip-flops.

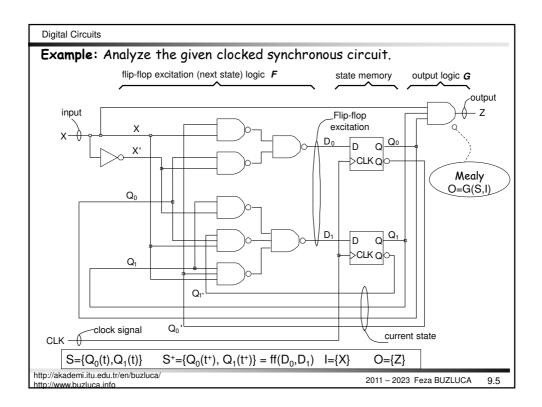
The functional behavior of a latch or flip-flop can be described by a **characteristic equation** that specifies the flip-flop's next state as a function of its inputs and current state.

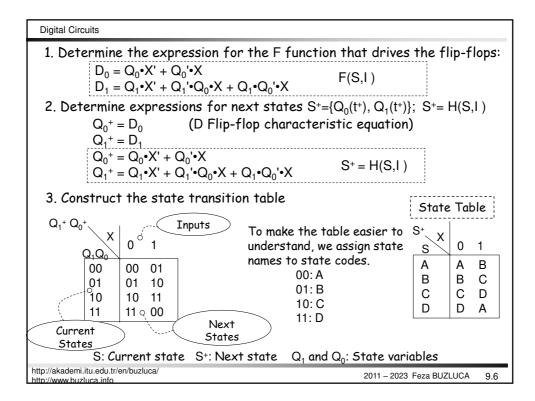
Characteristic equations for the flip-flops:

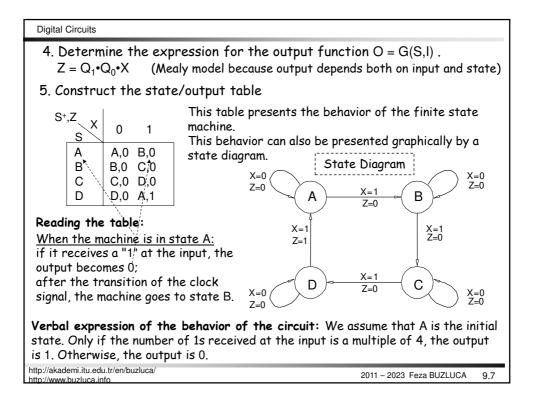
S-R FF : $Q(t+1) = S + \overline{R} \cdot Q(t)$ (SR = 0)J-K FF : $Q(t+1) = J \cdot \overline{Q(t)} + \overline{K} \cdot Q(t)$ D FF :Q(t+1) = DT FF : $Q(t+1) = T \oplus Q(t)$

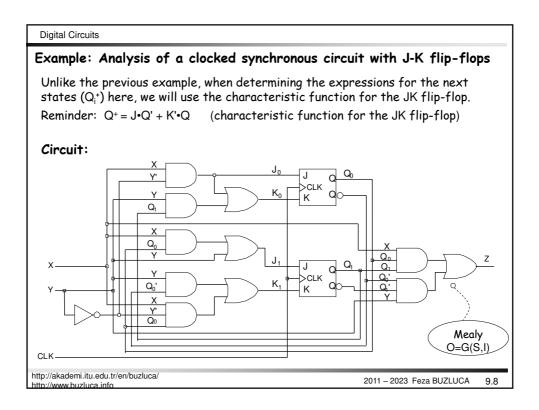
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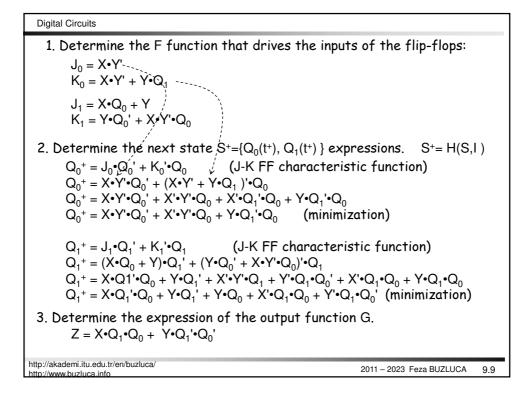
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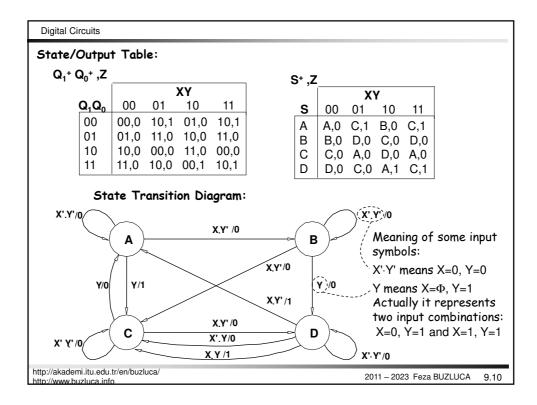


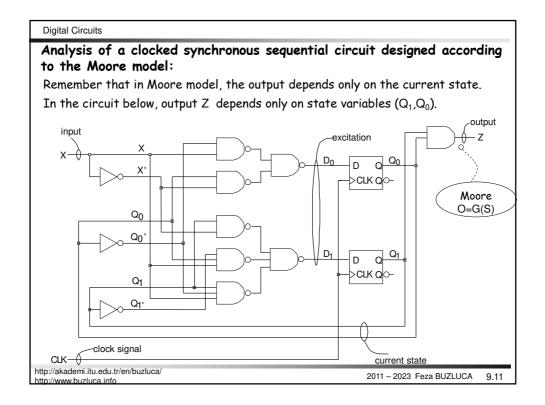




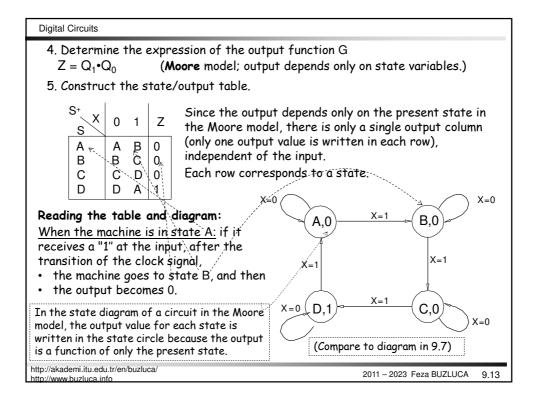




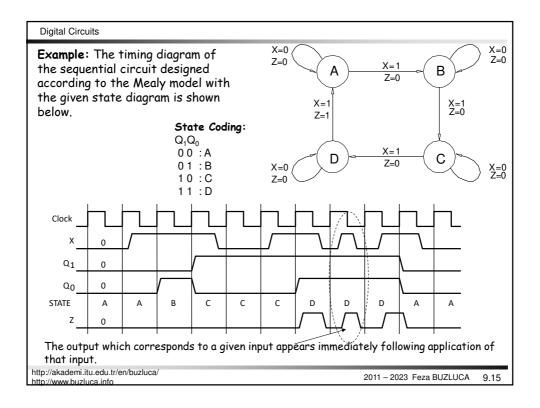




Digital Circuits		
The analysis of circuits designed according to the Moore model is very similar to that of circuits designed according to the Mealy model.		
They differ only in the construction and interpretation of the state/output table.		
1. Determine the expression for the F function that drives the flip-flops:		
$D_0 = Q_0 \bullet X' + Q_0' \bullet X$		
$D_1 = Q_1 \cdot X' + Q_1' \cdot Q_0 \cdot X + Q_1 \cdot Q_0' \cdot X$		
2. Determine the next state $S^+=\{Q_0(t^+), Q_1(t^+)\}$ expressions. $S^+=H(S,I)$		
$Q_0^+ = D_0^-$		
$Q_1^+ = D_1^-$		
$\mathbf{Q}_{0}^{+} = \mathbf{Q}_{0}^{\bullet} \mathbf{X}' + \mathbf{Q}_{0}^{\bullet} \mathbf{X}$		
$Q_{1}^{+} = Q_{1}^{\bullet}X' + Q_{1}^{'}Q_{0}^{\bullet}X + Q_{1}^{\bullet}Q_{0}^{'\bullet}X$		
3. Construct the transition table and the state table.		
$Q_{1^{+}}Q_{0^{+}}$	S ⁺ , v	
$A = \begin{bmatrix} X \\ Q_1 Q_0 \end{bmatrix} = \begin{bmatrix} X \\ 0 \end{bmatrix} = \begin{bmatrix} X \\ 0 \end{bmatrix}$	s × 0 1	
00 00 01 For simplicity, letters of	A A B	
01 01 10 the alphabet are	B B C	
10 10 11 assigned to state codes.	C C D	
11 11 00	D D A	
S: Current state S ⁺ : Next state Q_1 and Q_0 : State variables		
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Digital Circuits	
Interpretation of Outputs in Mealy and Moore Models If you check the output of a digital circuit at a certain moment, you will always read a logical 0 or 1 (except high impedance outputs).	
However, this value may not be valid due to some reasons. For example, due to internal delays, the circuit might not have finished its job, yet.	
Therefore, it is important when to read (sample) the output.	
In clocked synchronous sequential circuits, outputs are sampled (read) at different times depending on the model (Mealy or Moore).	
Mealy Model:	
Since the output depends also on the input, if the input changes, the output changes at the same time (actually, after the propagation delay).	
A circuit designed using the Mealy model operates as follows:	
1. Input values (I) are applied.	
2. Output values are obtained as a function of the input and current state. $O=G(S,I)$	
3. The active edge of the clock signal (for example, rising edge (0 to 1 transition)) arrives at the flip-flops.	
4. The machine goes to the next state. The next state is a function of the input and current state. $S^+{=}H(S,I)$	
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Digital Circuits

Moore Model:

In the Moore model, since the output is the function of the state only, change in the input cannot affect the output immediately.

The effect of changes in input can be seen on the output just after the change in the state.

A circuit designed using the Moore model operates as follows:

- 1. Input values (I) are applied.
- 2. The active edge of the clock signal (for example, rising edge (0 to 1 transition)) arrives at the flip-flops.
- 3. The machine goes to the next state. The next state is a function of the input and current state. $S^+{=}H(S{,}I)$
- 4. The output value is determined as a function of the new state. $O\!=\!G(S)$

In the Moore model, the output which results from application of a given input does not appear until after the clock pulse.

Therefore, the output sequence is displaced in time with respect to the input sequence.

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